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Comparison of Retention Modeling in Ion Chromatography by Using Multiple Linear Regression and Artificial Neural Networks

Tomislav Bolanča and Štefica Cerjan-Stefanović

University of Zagreb, Faculty of Chemical Engineering and Technology,
Department for Analytical Chemistry, Zagreb, Croatia

Goran Srečnik

PLIVA, Pharmaceutical Industry, Research and Development, Zagreb,
Croatia

Željko Debeljak

Clinical Hospital Osijek, Department of Medicinal Biochemistry, Osijek,
Croatia

Milko Novič

National Institute of Chemistry, Laboratory for Analytical Chemistry,
Ljubljana, Slovenia

Abstract: The aim of this work is comparison of the prediction power of multiple linear regression and artificial neural networks retention models for inorganic anions (fluoride, chloride, nitrite, sulfate, bromide, nitrate, and phosphate) in suppressed ion chromatography with isocratic elution. Relations between ion chromatographic parameters (eluent flow rate and concentration of OH^- in eluent) and retention time of particular anion are described with unique mathematical function obtained by multiple linear regression and with a three-layers feed-forward artificial neural network. The artificial neural network was trained with a Levenberg-Marquardt

batch error back propagation algorithm. It is shown that the multiple linear regression retention model has lower, but still very satisfactory, predictive ability. Due to its complexity, the artificial neural network must still be regarded as a more complicated technique. That indicates multiple linear regression as a method of choice for retention modeling in the case of ion chromatographic analysis with isocratic elution.

Keywords: Ion chromatography, retention modeling, multiple linear regression, artificial neural networks

INTRODUCTION

Ion chromatography (IC) is a widely used technique and its methodology and applications are described in several books (1, 2) and reviews (3–8). Method development in ion chromatography is relatively complex owing to the great number of parameters that influence separation, i.e., concentration and type of eluent ions, eluent flow rate, and temperature. The optimal separation in ion chromatography can be achieved by using computer-assisted optimization procedures that are based on a retention model providing a mathematical relationship for calculating the retention time of the analyte under differing conditions. The predictive ability of the retention model is the most important consideration in the success of the separation optimization procedure.

Two types of retention models can be identified, namely, theoretical (hard modeling) (9–19) and empirical (soft modeling) (20–23). Theoretical models are derived totally from theory and invariably require at least knowledge of parameters relating to the analyte, stationary phase, and eluent before calculation of the analyte retention factor is possible. Empirical models are not based on theoretical explanations of the physical and chemical interactions. They concentrate on finding the best relation between controlled and measured parameters. The main advantages of empirical modeling are the accuracy and speed of the algorithms, while the main disadvantage is that there is no theoretical explanation of occurred interactions.

Comparison of a series of mathematical models of retention in ion chromatography with special emphasis on the separation of anions were discussed earlier (9, 10, 21). The linear solvent strength model in both its multiple eluent species forms, the dominant equilibrium approach, the competing ion effective charge approach, the Hoover model, the dual eluent species model, the Kuwamoto model, the extended dual eluent species model, the multiple species eluent/analyte model, and the empirical end of points model were examined. It was shown that the more complex the model is, the more improved the prediction is, but none of the models is satisfactory for implementation in software. An empirical end of points model in which linear relationship is assumed between logarithm of capacity factor ($\log k$)

and log (eluent) but the slope, which is determined experimentally, gave the best performance. A comparison between empirical retention models in which the relationship between log k and the volume fraction of the organic modifier in the eluent as well as $1/k$ and volume fraction of the organic modifier in micellar liquid chromatography was published (24, 25). It is shown that the retention model relating $1/k$ and volume fraction of the organic modifier gave best performance.

The use of the machine learning methods for empirical retention modeling represents the fundamental research issue. The ability of a computer to learn independently is a recognized manifestation of intelligence and offers the potential to build intelligent systems more efficiently. There are many different approaches one can take to develop a method of machine learning. Techniques that are currently popular include artificial neural networks (ANN), genetic algorithms (GA), and induction (26). Retention models obtained by using artificial neural networks have very good predictive ability, but described algorithms are complex and require more than basic knowledge about artificial neural network theory (20, 22, 23). That is why it is essential to develop more user friendly mathematical methods to model ion chromatographic retention time without a significant decrease in predictive ability.

The objective of this work is the development of a simple and rapid methodology for empirical retention modeling of seven inorganic anions (fluoride, chloride, nitrite, sulfate, bromide, nitrate, and phosphate) in suppressed ion chromatography with isocratic elution. Relations between ion chromatographic parameters (eluent flow rate and concentration of OH^- in eluent) and retention time of particular anions are described with unique mathematical functions and with artificial neural networks. Coefficients of the functions were found by using multiple linear regressions. The unique technique of experimental data selection for modeling set was used, allowing improvement of multiple linear regression and artificial neural network models' prediction power. Prediction power of retention models is validated with an external set of experimental data points and compared. It is shown that the developed multiple linear regression retention model offers less complex and rapid alternative for retention modeling with fairly good predictive ability.

EXPERIMENTAL

Reagents

Stock solutions of fluoride (1.0000 g/L), chloride (1.0000 g/L), nitrite (1.0000 g/L), sulfate (1.0000 g/L), bromide (1.0000 g/L), nitrate (1.0000 g/L), and phosphate (1.0000 g/L) were prepared from the air-dried (at 105°C) salts of individual anions of p.a. grade (Merck, Darmstadt, Germany). Working standard solutions of fluoride (2.00 mg/L), chloride (5.00 mg/L),

nitrite (10.00 mg/L), sulfate (10.00 mg/L), bromide (20.00 mg/L), nitrate (20.00 mg/L), and phosphate (30.00 mg/L) were prepared by measuring the appropriate volume of stock solution of the individual anion onto a 100 mL volumetric flask, which was later filled to the mark with Milli-Q water. Working eluent solutions were prepared online by appropriate dilution of KOH with Milli-Q water. An $18\,M\Omega cm^{-1}$ water (Millipore, Bedford, MA, USA) was used for dilution in all cases.

Apparatus

The Dionex DX500 chromatography system (Dionex, Sunnyvale, CA, USA) equipped with quarternary gradient pump (GP50), eluent generator module (EG40), chromatography module (LC25), and detector module (ED40) was used in all experiments. Separation and suppressor columns used were the Dionex IonPac AG15 (4×50 mm) guard column, the IonPac AS15 (4×250 mm) separation column, and the ASRS-ULTRA-4 mm suppressor column, working in recycle mode, respectively. The sample-loop volume was 50 μL. The eluent flow rates were 1.00 to 1.95 mL/min, and concentrations of OH^- in eluent were 25.00 to 60.00 mmol/L. The whole system was computer controlled through PeakNet 5.1 software. The applied chromatography setup is schematically presented in Fig. 1.

The data for further evaluation were obtained by exporting the appropriate chromatograms into ASCII files. ASCII data files were further evaluated using a Microcal Origin (Microcal Software, USA) software package.

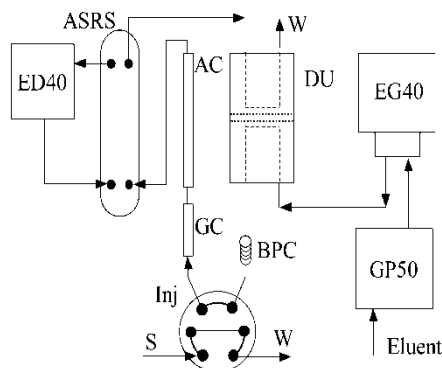**Figure 1.** The scheme of the DX500 ion chromatography system with built-in electro-dyalitic KOH generator (EG40). GP50, quaternary gradient pump; EG40, eluent generator; DG, degas module; Inj, injector; GC, guard column (AG15); AC, analytical column (AS15), ASRS, suppressor column (ASRS-ULTRA, recycle mode); BPC, back-pressure coil; ED40, electrochemical detector (conductivity mode); S, sample; eluent, OH^-, and W, waste.

Experimental Design

The experimental design was planned to describe the chromatographic behavior in a multidimensional space: retention time vs. eluent flow rate and concentration of OH^- in eluent. The eluent flow rate varied in range from 1.00 to 1.95 mL/min and the concentration of OH^- in eluent varied from 25.00 to 60.00 mmol/L. The 128 experimental data points were obtained. The experimental data points are logarithmically ($\log_{10}$) transformed before modeling, because of the hetroscedastic nature of the retention times variance. That provides the homogeneous variance in output of the multiple linear regresion retention model (retention times of fluoride, chloride, nitrite, sulfate, bromide, nitrate, and phosphate).

The independent set for modeling (16 experimental data points, Table 1) and for validating (112 experimental data points) were selected to cover the whole design space. For that purpose the design space (128 experimental data points) was divided into 16 subspaces from which one experimental data point was chosen for the modeling set from each subspace by using random function. The remaining 112 experimental data points were used as a validation set. Figure 2 presents the experimental design model where the 16 experimental data points used for modeling set are marked.

Retention Modeling

Relations between retention times of a particular anion [f(x), i.e., retention time of: fluoride, chloride, nitrite, sulfate, bromide, nitrate, and phosphate] and ion chromatographic parameters (x_1 = elunet flow rate and x_2 = concentration of OH^- in eluent) were described with the unique mathematical function:

$$f(x) = a_0 + a_1 x_1 + a_2 x_2 + a_3 \frac{1}{x_1} + a_4 \frac{1}{x_2} + a_5 x_1 x_2 \tag{1}$$

The main advantages of the proposed model are the inverse proportional relation between retention time and eluent flow and retention time and concentration of OH^- in eluent. The presented equation is proposed on the basis of retention modeling experiences in micellar liquid chromatography (24, 25). The retention model with one function that takes into account all seven inorganic anions is very hard to achieve. Therefore, retention times of inorganic anions were modeled separately. Constants a_0, a_1, a_2, a_3, a_4, and a_5 were determined in order to reduce deviation of the model by using multiple linear regression.

The neural network used in this paper is the feed-forward back-propagation neural network. The input layer consists of the two nodes

Table 1. Experimental data points used for determination of retention model function coefficients by using multiple linear regression and artificial neural network retention model training calculations

| Eluent flow rate/mL/min	$c(OH^-)$ in eluent/ mmol/L	Fluoride/ min	Chloride/ min	Nitrite/min	Sulfate/min	Bromide/ min	Nitrate/min	Phosphate/min
1.55	25	4.53	7.52	9.02	15.43	15.93	17.48	47.53
1.4	30	4.6	7.53	9.03	13.48	15.55	17.62	35.45
1.15	32	5.05	8.25	9.87	14.12	16.85	19.03	34.53
1.65	32	4.15	6.35	7.45	10.37	12.22	13.67	24.28
1.3	34	4.67	7.47	8.9	12.02	15.12	17.05	28.18
1.75	36	3.9	5.72	6.63	8.38	10.57	11.78	17.23
1.3	38	4.57	7.08	8.37	10.32	13.97	15.68	21.65
1.15	40	4.82	7.4	8.72	10.37	14.35	16.07	20.42
1.1	42	4.92	7.63	9.05	10.45	15.1	16.93	20.33
1.3	42	4.48	6.77	7.95	9.08	13.03	14.58	17.23
1.75	44	3.77	5.28	6.03	6.65	9.28	10.27	11.22
1.6	46	3.97	5.67	6.55	7	10.33	11.43	11.7
1.3	50	4.35	6.3	7.3	7.48	11.62	11.98	12.93
1	55	4.62	4.97	7.3	8.47	12.95	13.68	15.23
1.5	55	3.95	5.43	6.17	6.17	8.73	9.47	10.43
1.4	60	4.08	5.62	6.05	6.38	8.28	9.77	10.73
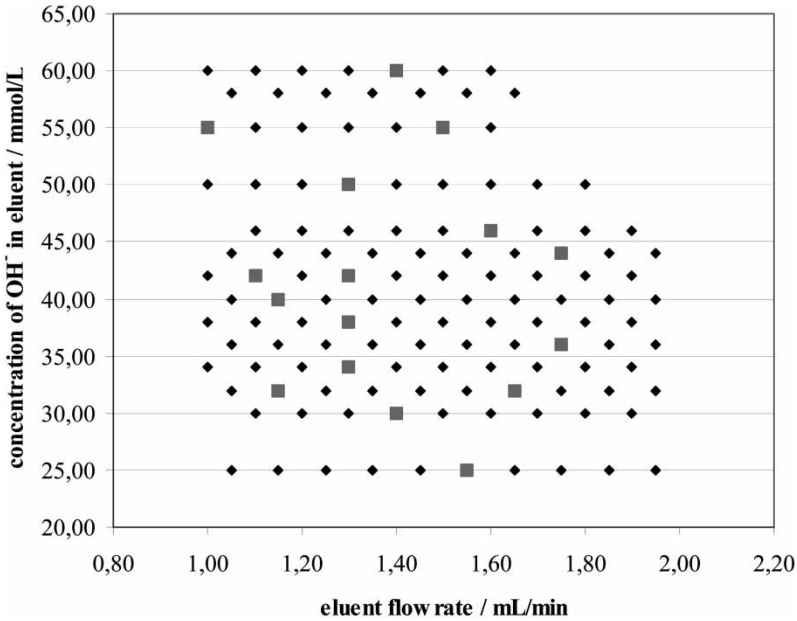
Figure 2. Design of 128 experimental data points: concentration of OH⁻ in eluent vs. eluent flow rate. The 16 experimental data points used for retention modeling are marked.

representing eluent flow rate and concentration of OH⁻ in eluent. The output layer consists of seven nodes representing retention times of the seven inorganic anions (fluoride, chloride, nitrite, sulfate, bromide, nitrate, and phosphate).

The neural network consists of one hidden layer of nodes. Two different transfer functions were used. The hyperbolic tangent sigmoid transfer function was used for computation of hidden layer nodes activities:

$$\Theta(x_i * W) = \frac{1 - e^{-x_i * W}}{1 + e^{-x_i * W}} \tag{2}$$

where θ represents the transfer function, x represents the input vector, and W represents the weigh vector. For computation of output activities, the linear transfer function was employed:

$$\Theta(x_i * W) = x_i * W \tag{3}$$

The Levenberg-Marquardt batch learning procedures using momentum were applied, and the number of hidden layer nodes and the number of iteration steps used for training procedures was optimized, leading to the best possible description of retention behavior.

The program for multiple linear regression and artificial neural networks retention models was created by the authors on the MATLAB environment (MATLAB 6.0, MathWorks, Sherborn, MA, USA). All the calculations were performed on an IBM compatible personal computer equipped with a 266 MHz Pentium IV processor and 512 Mb RAM.

RESULTS AND DISCUSSION

The results of application of multiple linear regression for calculation of coefficients of the proposed equation are shown in Table 2. The interpretation of the resulting equation is in terms of the relative contributions of independent variables (eluent flow rate and concentration of OH^- in eluent) to the response (retention time of particular anion). It can be seen (Table 2) that the concentration of OH^- in eluent (a_4) has a particularly large influence on retention of sulfate and phosphate. This is due to the fact that the ionic form of sulfate and phosphate in solution depends on pH value. Retentions of fluoride, chloride, nitrite, and nitrate also are the most influenced by concentration of KOH in eluent (a_4), while bromide is most influenced by eluent flow rate (a_3). This shows that bromide has a nearly constant affinity towards the stationary phase. The second largest influence on retention is eluent flow rate (a_3). The large values of a_4 and a_3 coefficients justify the inverse proportional relation between retention time and concentration of OH^- in eluent and retention time and eluent flow rate. It also can be seen that the term ($x_1{}^*x_2$), which shows the influence of eluent flow rate on concentration of OH^- in eluent, cannot be neglected since a_5 has considerable value.

From Table 2 it can be seen that correlation coefficients are greater than 0.988, which is a very satisfactory value. But, those coefficients of correlation represent deviations of 16 experimental data points used for multiple linear regression retention modeling calculations from the calculated retention model itself. They do not represent the deviation of the retention model from the actual ion chromatographic retention behavior. For that reason the validation of the proposed retention model with the experimental data set that was not used for modeling procedure was applied.

The artificial neural network model was optimized in terms of obtaining a precise and accurate retention model. From Fig. 3, it can be seen that minimal relative error of the proposed neural network retention model is obtained by using three hidden layer nodes and 300 iteration steps. It is also shown that the number of iteration steps has a low influence on relative error, particularly in comparison with influences that have a number of hidden layer nodes on relative error. However, one of the important factor that has to be considered is reducing computation time. If the number of iteration steps is higher, the computation time is longer. That fact only confirms the previous conclusion that the optimal number of iteration steps is 300. From Fig. 4 it can be seen

Table 2. Retention model equation coefficients calculated by using multiple linear regression. 16 Experimental data points were used for calculations

|	Fluoride	Chloride	Nitrite	Sulfate	Bromide	Nitrate	Phosphate
Coefficients of the equation							
a_0	0.4980	0.6746	0.8319	0.5781	1.1562	1.3275	0.1925
a_1	−0.0832	−0.0999	−0.0841	−0.1981	−0.0084	−0.0796	−0.2546
a_2	−0.0014	−0.0023	−0.0041	−0.004	−0.0061	−0.0059	−0.0011
a_3	0.2458	0.2963	0.3343	0.3081	0.4078	0.2987	0.3964
a_4	3.0221	4.8528	3.0933	18.3406	−0.0019	0.9958	38.3015
a_5	0.0010	0.0006	0.0003	0.0024	−0.0018	−0.0014	0.0038
Correlation coefficients	0.9988	0.9974	0.9953	0.9973	0.9880	0.9928	0.9927
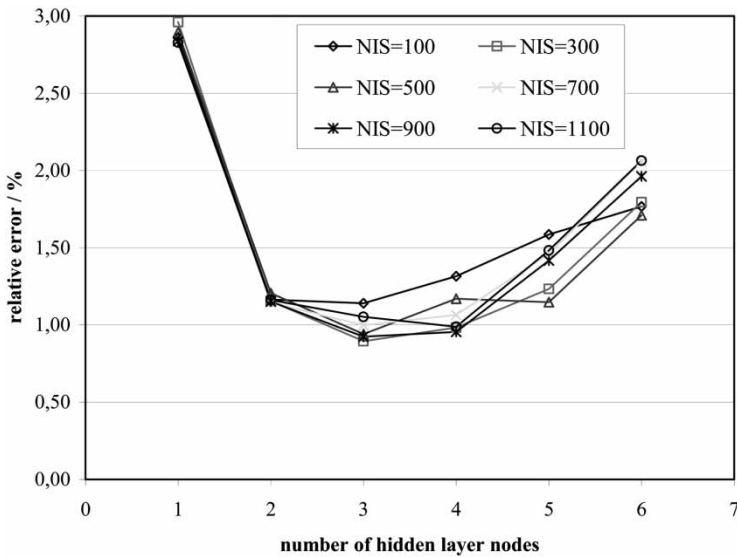
Figure 3. Optimization of artificial neural network retention model. Relative error against number of hidden layer nodes obtained by using different number of iteration steps (NIS).

that number of experimental data points used for the training set has significant influence on selection of optimal parameters (number of hidden layer nodes and number of iteration steps) for the artificial neural network retention model. Reducing the number of experimental data points used for the training set is crucial for development of a retention model without loosing time on unnecessary experimentation. It is also important that the small number of experimental points in the training set do not decrease the predictive ability of the retention model. From Fig. 4 it can be seen that the relative error has higher values if is used with a small number of experimental data points for training set (8, 12, or 16 experimental data points). When using more experimental data points for the training set (16, 19, 22, 26, or 32 experimental data points) relative error has a smaller, but nearly the same, value. It can be concluded that the optimal number of experimental data points used for training set is 16. The optimal artificial neural network retention model was obtained by using 16 experimental data points in a training set identical to the experimental data set used for multiple linear regression retention modeling. The obtained artificial neural network retention model was validated with an external set of data identical to multiple linear regression validation set.

The amount of knowledge and time spent to develop the multiple linear regression retention model is significantly lower than that needed to
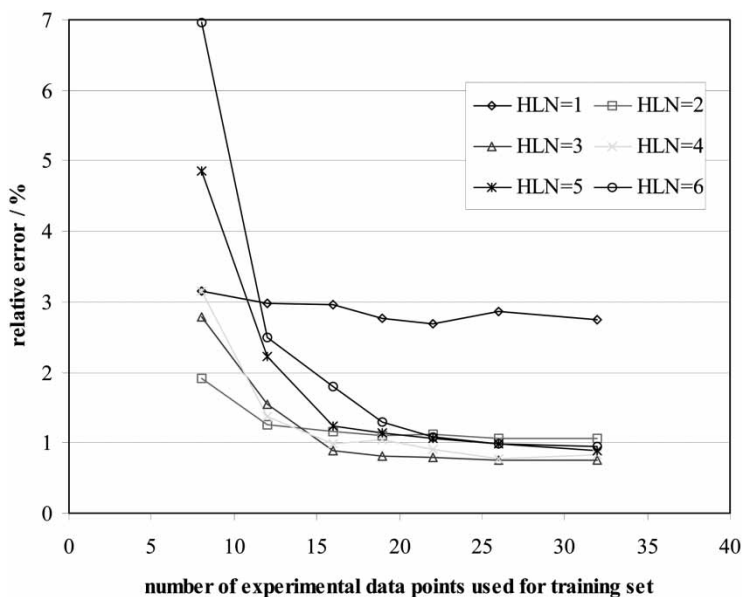
Figure 4. Optimization of artificial neural network retention model. Relative error against number of experimental data points used for training set obtained by using different numbers of hidden layer nodes (HLN).

develop an artificial neural network retention model. Multiple linear regression calculations need knowledge of sophisticated linear algebra, which includes the calculation of sub- and inversion matrices. Artificial neural network calculations, along with knowledge of the calculation of sub- and inversion matrices, require knowledge of nonlinear optimization, which includes the calculations of Hessian and Jacobian matrices. The amount of knowledge needed to develop one artificial neural network retention model which describes retention times of all seven inorganic anions, is nearly similar to the amount of knowledge needed to develop separate ANN retention models for each anion. However, time used for modeling is significantly lower if only one artificial neural network retention model has to be developed. It is due to the fact that in this particular case of retention modeling, a neural network with two inputs and seven outputs is not much more complex then a neural network with two inputs and one output.

The prediction power of the multiple linear regression retention model can be comparable to the artificial neural network retention model if the prediction power calculations are based on an external set of experimental data. The prediction powers of developed models were tested and results are shown on Figs. 5 and 6. The figures show that relationships between simulated retention times (y) against measured retention times (x) were investigated.
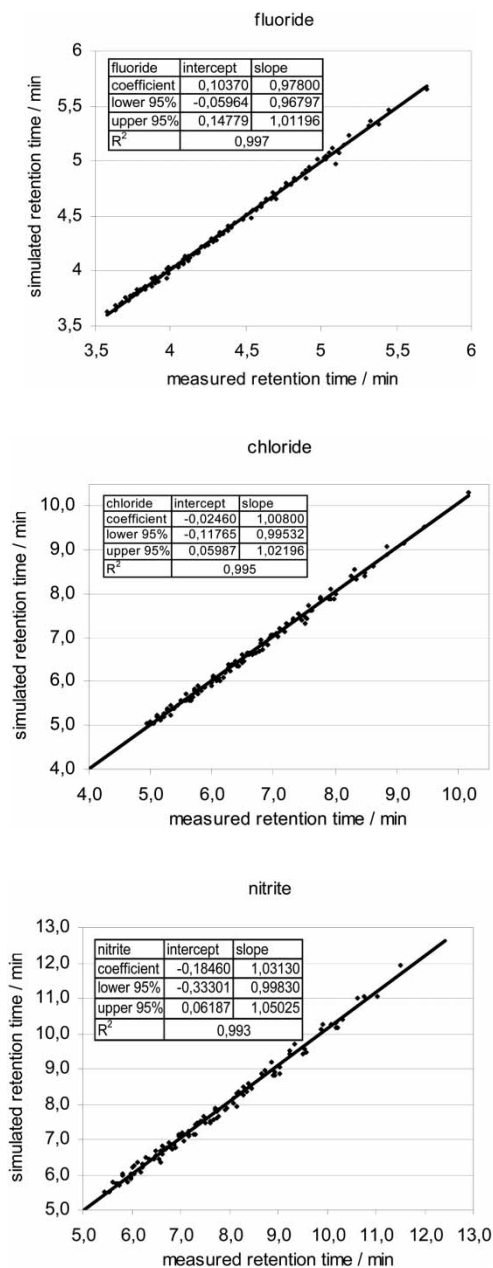
Figure 5. Validation results of multiple linear regression retention model obtained by using external experimental data set. The 112 experimental data points were used for calculations.

sulfate

sulfate	intercept	slope
coefficient	-0,49820	1,05320
lower 95%	-0,18719	0,99720
upper 95%	0,00087	1,02590
R^2		0,984

bromide

bromide	intercept	slope
coefficient	-0,09800	1,01770
lower 95%	-0,89510	0,98710
upper 95%	0,22269	1,08447
R^2		0,997

nitrate

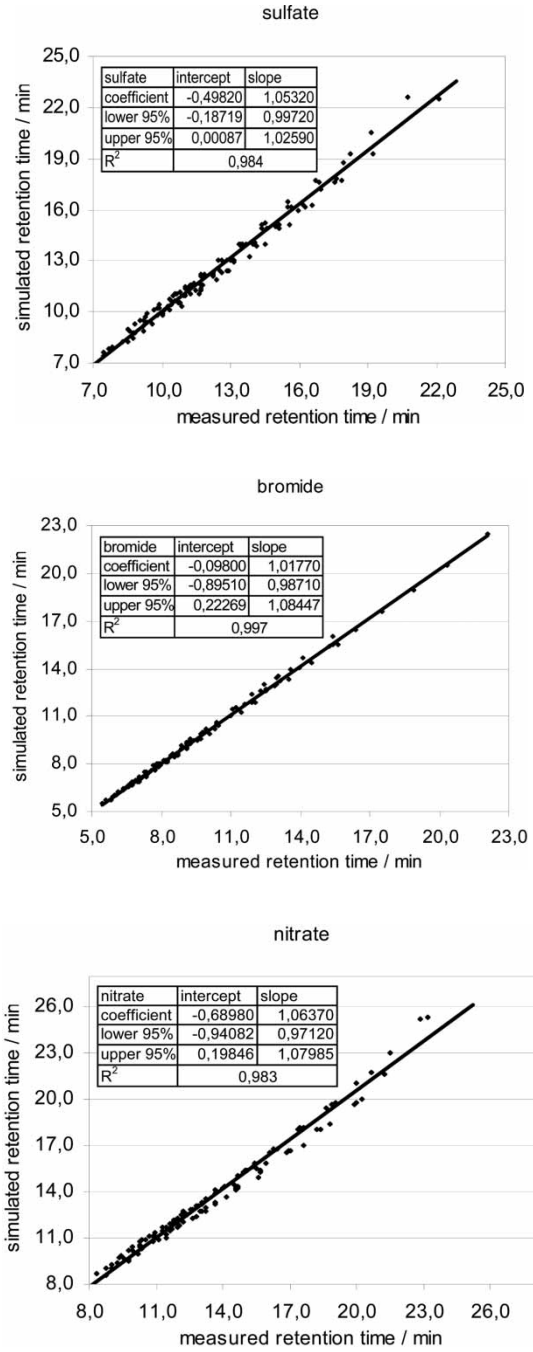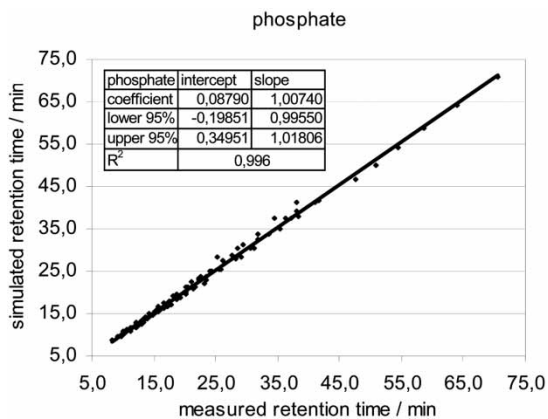| nitrate	intercept	slope
coefficient	-0,68980	1,06370
lower 95%	-0,94082	0,97120
upper 95%	0,19846	1,07985
R^2		0,983

Figure 5.   Continued.

Figure 5.   Continued.

If there are no modeling errors and no measurement random errors were made, and if there were no bias, this would yield the relationship y = x. Because at least random errors were made, the coefficients of linear relationship were different (intercept was different from zero and/or slope was different from one). There are four possibilities, namely:

- if intercept is equal to zero and slope is equal to one, there is no systematic error.
- if intercept is equal to zero and slope is different from one, there is a proportional systematic error.
- if intercept is different from zero and slope is equal to one, there is absolute systematic error.
- if there is no linearity, it is necessary to carry out the modeling over a shorter ion chromatographic parameter range (if this is still compatible with original aim).

It can be seen from Figs. 5 and 6 that lower and upper 95% confidence interval limit boundaries for intercept include value zero. This proves that intercept is not significantly different from zero with respect to a confidence interval of 95%. Furthermore, lower and upper 95% confidence interval limit boundaries for slope include value one, which proves that slope is not significantly different from one with a confidence interval of 95%. On the basis of previous discussion it can be stated that there is no systematic error present in optimized artificial neural network retention models for all anions.

From Fig. 7 it can be seen that the multiple linear regression retention model provides the best results for modeling fluoride and chloride retention
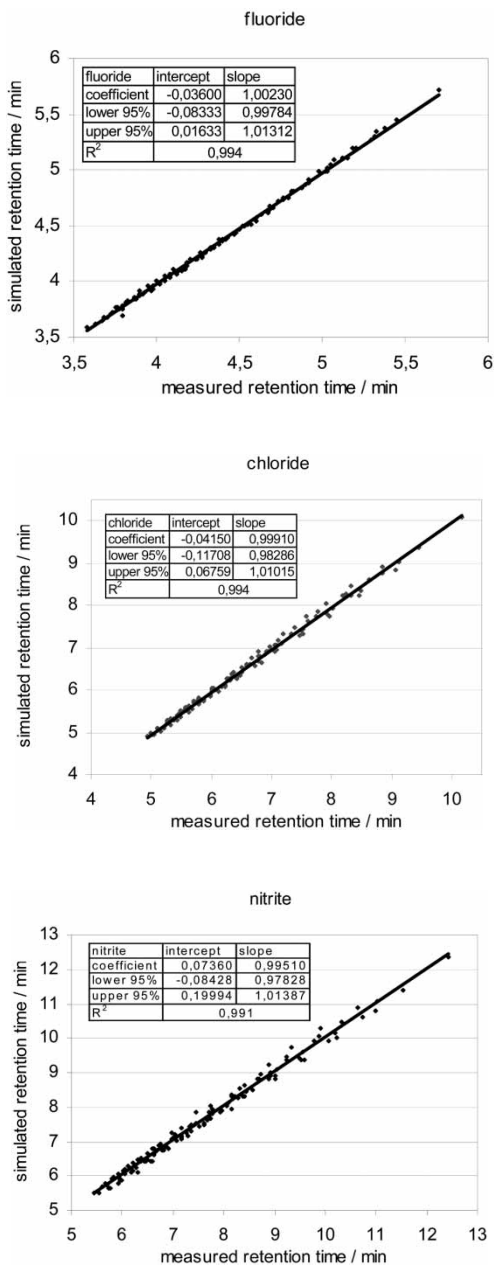
fluoride

fluoride	intercept	slope
coefficient	-0,03600	1,00230
lower 95%	-0,08333	0,99784
upper 95%	0,01633	1,01312
R^2		0,994

chloride

chloride	intercept	slope
coefficient	-0,04150	0,99910
lower 95%	-0,11708	0,98286
upper 95%	0,06759	1,01015
R^2		0,994

nitrite

nitrite	intercept	slope
coefficient	0,07360	0,99510
lower 95%	-0,08428	0,97828
upper 95%	0,19994	1,01387
R^2		0,991

Figure 6. Validation results of artificial neural network retention model obtained by using an external experimental data set. The 112 experimental data points were used for calculations.
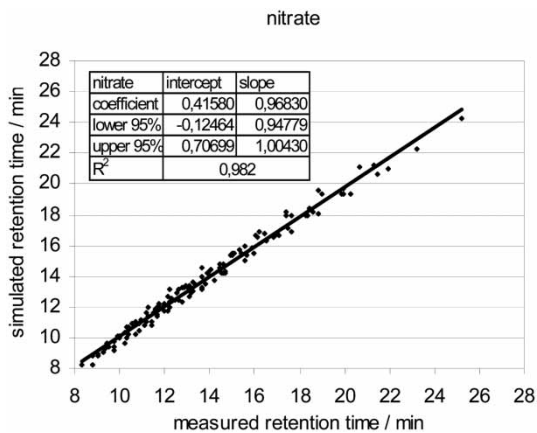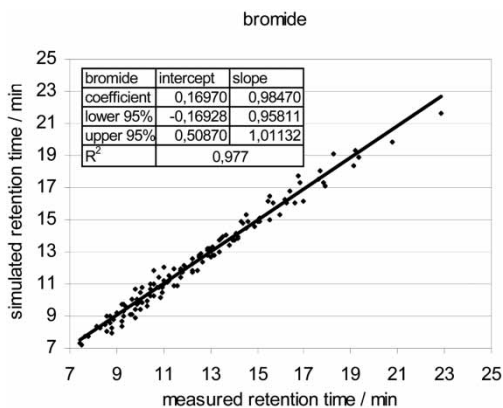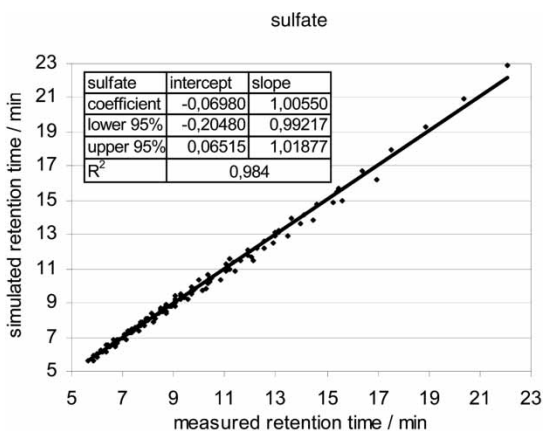
sulfate

sulfate	intercept	slope
coefficient	-0,06980	1,00550
lower 95%	-0,20480	0,99217
upper 95%	0,06515	1,01877
R^2	0,984	

bromide

bromide	intercept	slope
coefficient	0,16970	0,98470
lower 95%	-0,16928	0,95811
upper 95%	0,50870	1,01132
R^2	0,977	

nitrate

nitrate	intercept	slope
coefficient	0,41580	0,96830
lower 95%	-0,12464	0,94779
upper 95%	0,70699	1,00430
R^2	0,982	

Figure 6.   Continued.

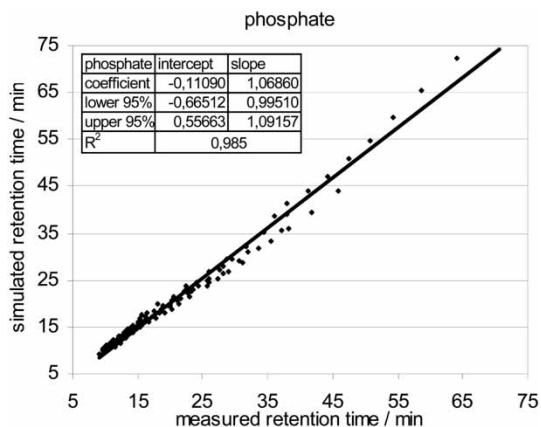| phosphate	intercept	slope
coefficient	-0,11090	1,06860
lower 95%	-0,66512	0,99510
upper 95%	0,55663	1,09157
R^2	0,985	

Figure 6. Continued.

($R^2 = 0.994$) followed by nitrite ($R^2 = 0.994$). Prediction power for retention of phosphate ($R^2 = 0.985$), sulfate ($R^2 = 0.984$), and nitrate ($R^2 = 0.982$) is also very satisfactory and the lower prediction ability of the multiple linear regression retention model is obtained for bromide ($R^2 = 0.977$). Figure 7 shows that nearly the same predictive power of an artificial neural network retention model is obtained for fluoride and bromide ($R^2 = 0.997$), phosphate ($R^2 = 0.996$), chloride ($R^2 = 0.995$), and nitrite ($R^2 = 0.993$). Prediction power for sulfate ($R^2 = 0.984$) and nitrate ($R^2 = 0.983$) is only slightly lower.
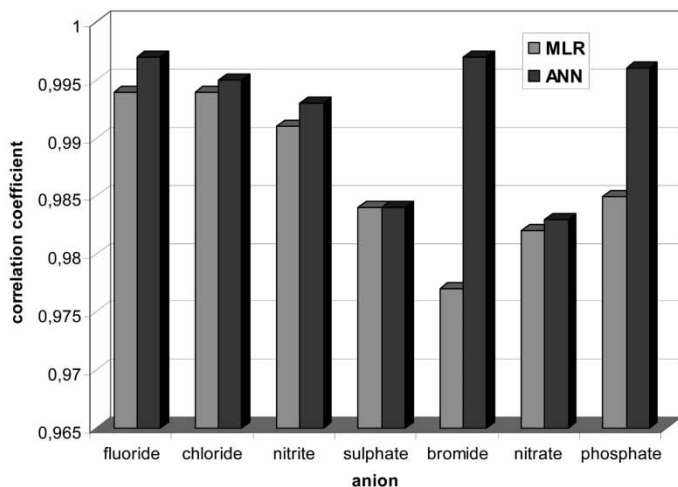

Figure 7. Comparison of retention models developed by using multiple linear regression and by using artificial neural networks.

By summarizing the results from Figs. 5, 6, and 7, it can be stated that the artificial neural network retention model has better ability to predict retention times of each and every modeled anion. However, both of the models show very good predictive ability. It can be concluded that for ion chromatographic separation with isocratic elution it is possible to apply the multiple linear regression retention model without making significant errors in global optimization of separation (retention modeling) procedure.

CONCLUSIONS

This study describes development of multiple linear regression and artificial neural network retention models that can be used for resolving separation problems in ion chromatography with isocratic elution. To underline the advantages of the proposed methodology, the multiple linear regression retention model was compared to the artificial neural networks retention model. It is shown that the artificial neural network has better prediction ability, but correlation coefficients for multiple linear regression are still very satisfactory. Due to their complexity, artificial neural networks must be regarded as a more complicated technique compared to multiple linear regression. More than basic knowledge about artificial neural networks and computer programming is needed to create artificial neural network retention modeling and further optimization of separation in ion chromatography used at least, a time consuming process. Multiple linear regression retention modeling is less time consuming, simple to understand, and does not require theory knowledge about artificial neural networks and more sophisticated computer programming methodology. This information indicates multiple linear regression retention modeling as a preferred choice, convenient to use when simplicity and time spend for modeling is a more important factor then is slightly better predictive ability in global optimization of separation in ion chromatographic analysis with isocratic elution.

This study also shows that separation in ion chromatography with isocratic elution strongly depends on applied ion chromatographic conditions (eluent flow rate, concentration of OH^- in eluent). The developed retention models allow manipulating with the appearance of the particular peak on the chromatogram and allow improvement of separation between particular anions. By using those retention models, it is possible both to improve performance characteristics of the applied method and to speed up new method development by reducing unnecessary experimentation.

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